Numerical Analysis Numerical Solution of Linear System of Equations Sheet # 5



# Prob.1

Solve the following set of simultaneous linear equations by the matrix inverse method.

(a) 
$$2x + 3y - z = -10$$
,  
 $-x + 4y + 2z = -4$ ,  
 $2x - 2y + 5z = 35$   
(b)  $10x + 3y + 10z = 5$ ,  
 $8x - 2y + 9z = 2$ ,  
 $8x + y - 10z = 35$ 

## Prob.2

Solve the following of simultaneous equations using Gauss elimination method

(a) 
$$2x + y - 3z = 11$$
,  
 $4x - 2y + 3z = 8$ ,  
 $-2x + 2y - z = -6$   
(b)  $6x + 3y + 6z = 30$ ,  
 $2x + 3y + 3z = 17$ ,  
 $x + 2y + 2z = 11$   
(c)  $2x1 + x2 + x3 = 4$ ,  
 $3x2 - 3x3 = 0$ ,  
 $-x2 + 2x3 = 1$   
(d)  $x1 + 2x2 + 3x3 + 4x4 = 8$ ,  
 $2x1 - 2x2 - x3 - x4 = -3$ ,  
 $x1 - 3x2 + 4x3 - 4x4 = 8$ ,  
 $2x1 + 2x2 - 3x3 + 4x4 = -2$ 

## Prob. 3

Solve the following of simultaneous equations using Gauss Jordan method

(a) 
$$4x - 3y + 5z = 34$$
,  
 $2x - y - z = 6$ ,  
 $x + y + 4z = 15$   
(b)  $2x - y + z = -1$ ,  
 $3x + 3y + 9z = 0$ ,  
 $3x + 3y + 5z = 4$   
(c)  $x + y - z = 1$ .  
 $x + 2y - 2z = 0$ ,  
 $-2x + y + z = 1$   
(d)  $x - y = 2$ ,  
 $-2x + 2y - z = -1$ ,  
 $y - 2z = 6$   
(e)  $x + y + z = 3$ ,  
 $2x + 3y + z = 6$ ,  
 $x - y - z = -3$ 

### Prob. 4

Solve the following set of simultaneous linear equations using the Crout's method.

(a) 3x + 2y + 7z = 4, 2x + 3y + z = 5, 3x - 4y + z = 7 **Numerical Analysis Numerical Solution of Linear System of Equations** Sheet # 5



(*b*) x + y + z = 9, 2x - 3y + 4z = 13, 3x + y + 5z = 40(c) 2x + y - z = 6, x - 3y + 5z = 11, -x + 5y + 4z = 13Prob.5 (*a*) 2x - y + 5z = 15, 2x + y + z = 7,x + 3y + z = 10(b) 20x + y - 2z = 17, 3x + 20y - z = -18, 2x - 3y + 20z = 25(c) 5x + 2y + z = 12, x + 4y + 2z = 15,

### Solve the following of simultaneous equations using Jacobi method

x + 2y + 5z = 20

## Prob.6

Solve the following of simultaneous equations using Gauss-Seidal method and **Relaxation method** 

(a) 
$$4x - 3y + 5z = 34$$
,  
 $2x - y - z = 6$ ,  
 $z + y + 4z = 15$   
(b)  $2x - y + 5z = 15$ ,  
 $2x + y + z = 7$ ,  
 $x + 3y + z = 10$   
(c)  $15x + 3y - 2z = 85$ ,  
 $2x + 10y + z = 51$ ,  
 $x - 2y + 8z = 5$   
(d)  $10x1 - 2x2 - x3 - x4 = 3$ ,  
 $-2x1 + 10x2 - x3 - x4 = 15$ ,  
 $-x1 - x2 + 10x3 - 2x4 = 27$ ,  
 $-x1 - x2 - 2x3 + 10x4 = -9$   
200  
 $50$   
 $i_1$   
 $i_2$   
 $i_1$   
 $0 \vee 100$ 

The electrical network shown can be viewed as consisting of three loops. Applying Kirhoff's law ( $\sum$ voltage drops =  $\sum$  voltage sources) to each loop yields the following equations for the loop currents  $i_1$ ,  $i_2$ , and  $i_3$ :

Compute the three loop currents for R = 5, 10, and 20  $\Omega$ .

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